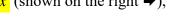
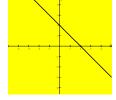
How to determine the portion and direction of a parametric curve when you are able to eliminate the parameter

Suppose you're given the parametric equations

parametric equations
$$x = 2 + t^2$$
$$y = -t^2$$

which corresponds to the rectangular equation y = 2 - x (shown on the right \Rightarrow),



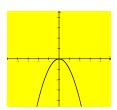


and you need to determine which part of the graph is being traced out and in what orientation.

1. Decide which parametric equation (x = or y =) you find easier to analyze.

$$y = -t^2$$
 will be easier

2. Sketch a graph of the function you chose in step 1, with the horizontal axis representing t, and the vertical axis representing whichever variable you chose in step 1 (in this case, y).



3. Describe what's happening on the graph in step 2 as t goes from $-\infty$ to ∞ (ie. as you move from left to right). Every time the graph changes general direction (from going up to going down, from going down to going up, or making a sudden discontinuous jump), describe that change (from what value to what value).

As
$$t$$
 goes from $-\infty$ to ∞ ,
 $y = -t^2$ goes from $-\infty$ to 0 to $-\infty$

4. Go to the graph of the original rectangular equation and identify which "points" on its graph correspond to the x- or y- values you found in step 3.

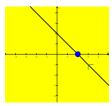
Remember that

 $x = -\infty$ corresponds to the far left side of the graph $y = -\infty$ corresponds to the bottom of the graph $x = \infty$ corresponds to the far right side of the graph $y = \infty$ corresponds to the top of the graph x = 0 corresponds to the y-intercept of the graph y = 0 corresponds to the x-intercept of the graph you can use the rectangular equation to find specific points

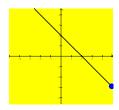
to the x – intercept (2,0)

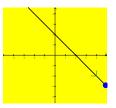
 $y = -t^2$ goes from $-\infty$ to 0 to $-\infty$, so the parametric curve goes from

the bottom of the graph of y = 2 - x

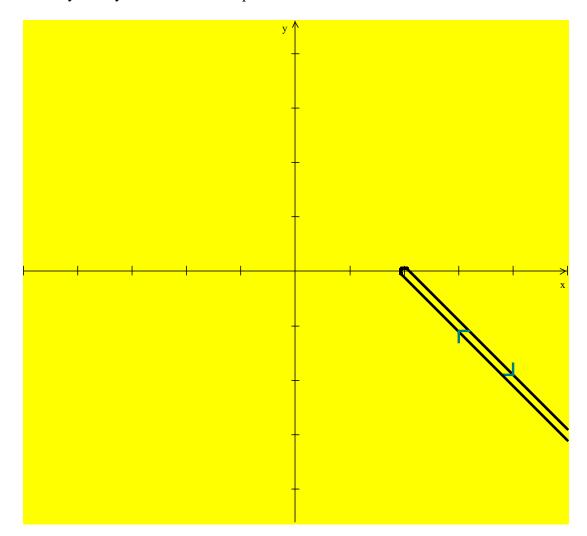


to the bottom





5. Sketch out only what you described in step 4.



YOUR TURN: (check using your calculator AFTER you have a solution)

- A. Analyze the parametric equations $x = -t^4$, which correspond to the rectangular equation $y = -x^2$, by analyzing the x = equation.
- B. Analyze the parametric equations $x = e^{-t}$, which correspond to the rectangular equation y = 2 x, by analyzing the x = equation.
- C. Analyze the parametric equations $x = e^{2t}$, which correspond to the rectangular equation $x = y^2$. You must decide which parametric equation to analyze (try both, but one will be easier than the other).
- D. Analyze the parametric equations $x = \sin t$, which correspond to the rectangular equation $y = 1 x^2$. You must decide which parametric equation to analyze.
- E. Analyze the parametric equations $x = 4 2 \ln t$. You must find the rectangular equation, and decide which parametric equation to analyze.